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Development of a distributed computing emulator

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Annotation

Taking distributed computing as a research area, this thesis focuses on the development of a new distributed computing emulator, which aims to cope with the deficiencies of existing emulators in terms of functionality and performance, and to meet the needs of emerging computing scenarios. The thesis firstly reviews the basic concepts and current status of distributed computing, analyzes the main features and challenges of current emulators, and demonstrates the necessity of developing a new type of emulator in the light of the technological development trend.

The theoretical part systematically introduces the key theories in distributed systems, including the logical time and order of events, the correctness proof of Lamport clocks and vector clocks, the consistency problem of distributed systems, and the Byzantine fault-tolerance mechanism, which provides theoretical support for the design and implementation of the emulator.

The software implementation part describes in detail the design and implementation of the behavior of distributed nodes in the FIFO channel oriented to the directed ring, and the development of the core module of the emulator is completed by using Python language. The design reliability and operational stability of the system are verified by analyzing and proving the correctness of the message processing flow.

The contribution of this research is to propose an efficient and scalable new distributed computing emulator that can adapt to the needs of complex distributed environments, and provide a powerful tool support for related research and practical applications. The paper concludes by summarizing the research results and looking forward to future improvements.

Keywords: distributed computing, emulator, logic clock, consistency

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1. State-of-the-Art and Motivation

1.1 Overview of Distributed Computing

Distributed computing refers to the coordination of multiple interconnected nodes to solve problems collaboratively. Each node, which may represent an independent computational device, communicates and exchanges information to contribute to a shared objective. This paradigm underpins many of today's essential systems, such as cloud platforms, distributed databases, and blockchain networks.

At its core, distributed computing is driven by the need to achieve scalability, fault tolerance, and efficient resource utilization. For instance:

Scalability allows systems to handle increasing workloads by adding more nodes.

Fault tolerance ensures system reliability despite hardware or network failures.

Resource optimization leverages the combined power of geographically distributed nodes to reduce operational costs[1].

Modern distributed systems have expanded far beyond traditional architectures.

Cloud-native applications now rely on microservices to enable flexible, modular systems. Blockchain technology employs decentralized ledgers to achieve trust and transparency. Meanwhile, edge computing shifts computation closer to data sources, reducing latency in applications like IoT and autonomous vehicles.

Despite these advancements, distributed computing introduces challenges related to:

- **Consistency:** Achieving agreement among nodes in the presence of failures or adversarial behavior.
- **Latency:** Managing communication delays in asynchronous environments.
- **Complexity:** Designing, implementing, and debugging distributed systems that involve non-deterministic behavior.

1.2 Distributed Computing Emulators

Distributed computing emulators simulate the behavior of distributed systems in controlled environments. These tools provide researchers, developers, and

educators with the ability to test algorithms, explore failure scenarios, and measure performance metrics without deploying physical clusters.

1.2.1 Current Emulators and Their Features

Several distributed computing emulators have emerged, each addressing specific needs:

Mininet:

Focus: Simulates network topologies and packet forwarding.

Strengths: Lightweight, supports rapid prototyping of networked systems.

Limitations: Focused on the networking layer, lacks support for application-layer protocols.

1. SimGrid:

Focus: Simulates large-scale distributed systems for studying scheduling and resource allocation.

Strengths: Accurate modeling of computational and communication delays.

Limitations: Limited debugging tools and visualization capabilities.

2. CORE (Common Open Research Emulator):

Focus: Emulates virtual networks for testing routing protocols.

Strengths: Flexible network configuration options.

Limitations: Primarily designed for networking experiments, not general-purpose distributed systems.

3. Blockchain-Specific Tools:

Ganache: Used for testing Ethereum smart contracts.

Hyperledger Caliper: Provides performance benchmarking for distributed ledger systems.

Limitation: Narrow focus on blockchain applications, unsuitable for broader distributed computing research.

1.2.2 Challenges in Current Emulators

While existing emulators are valuable, they often fall short in key areas:

1. Scalability: Simulating large-scale systems with thousands of nodes remains resource-intensive.
2. Specialization: Most tools are designed for specific use cases (e.g., networking or blockchain), limiting their adaptability to other domains.
3. Debugging and Visualization: Few emulators provide tools to visualize message flows, node states, or logical clock synchronization, making it difficult to identify and resolve issues.
4. User Accessibility: Many tools require expertise in configuration and deployment, posing a barrier for newcomers.

1.3 Emerging Trends and the Need for a New Emulator

As distributed systems evolve, new trends create additional demands for emulators:

1. Cloud-Native Architectures:

Microservices and containerized applications dominate modern distributed systems. Testing orchestration and fault tolerance in such environments requires support for dynamic node creation and teardown.

2. Blockchain and Decentralized Systems:

Distributed ledger technologies introduce unique challenges, such as achieving consensus in adversarial environments.

Emulators must simulate complex protocols like Proof of Work, Proof of Stake, and Byzantine Fault Tolerance.

3. Edge and IoT Computing:

Distributed systems now extend to edge devices, requiring emulators to handle resource-constrained nodes and intermittent connectivity.

4. AI and Machine Learning:

Distributed training of machine learning models involves synchronizing gradients across nodes.

Emulators must simulate high-bandwidth communication and heterogeneous hardware environments.

Given these trends, the need for a flexible, scalable, and user-friendly distributed computing emulator has become more pressing. Such a tool should:

- Support a wide range of distributed system architectures.
- Provide advanced debugging and visualization capabilities.
- Scale efficiently to simulate large systems.
- Be accessible to researchers, developers, and educators alike.

1.4 Motivation for Developing a New Distributed Computing Emulator

The motivation for creating a new emulator stems from the limitations of existing tools and the growing complexity of modern distributed systems. A new emulator could address these gaps by offering:

1. Scalability:

Efficient simulation of large-scale systems with thousands of nodes.

Dynamic adjustment of system parameters, such as network latency and failure rates[2].

2. Cross-Domain Applicability:

Flexibility to experiment with diverse systems, from blockchain networks to edge computing setups.

3. Debugging and Visualization:

Real-time visualization of node interactions, message flows, and logical clock synchronization.

Tools to analyze performance bottlenecks and identify causality violations.

4. Educational Value:

Simplified interfaces and pre-configured environments to teach distributed system concepts.

Hands-on experimentation with consensus protocols, logical clocks, and fault tolerance mechanisms.

5. Support for Modern Architectures:

Integration with containerized environments (e.g., Docker, Kubernetes) to model microservices.

Simulation of edge and IoT devices with constrained resources.

1.5 Proposed Contributions

The proposed emulator aims to offer a unified platform that overcomes the shortcomings of current tools[3]. Key features include:

- **Modularity:** Support for various distributed system models, including client-server, peer-to-peer, and hybrid architectures.
- **Scalability:** Efficient handling of large-scale simulations with configurable topologies and failure scenarios.
- **Advanced Debugging Tools:** Visualization of message queues, causal dependencies, and resource utilization.
- **User Accessibility:** Intuitive interfaces for rapid experimentation and compatibility with popular programming frameworks.

1.6 Conclusion

Distributed computing is a cornerstone of modern technology, but its complexity demands better tools for research, development, and education. Current emulators have made significant contributions but are often limited in scalability, adaptability, and usability. A next-generation distributed computing emulator has the potential to bridge this gap, providing a scalable, versatile, and user-friendly platform for tackling the challenges of modern distributed systems. By enabling experimentation and validation in a controlled environment, such an emulator could accelerate innovation across diverse domains, from blockchain to edge computing.

2. Theoretical Background

Distributed computing is a foundational field in computer science that enables independent nodes in a network to collaborate to solve problems that would be

infeasible for a single machine to handle. By distributing tasks and workloads across multiple nodes, these systems achieve enhanced scalability, fault tolerance, and efficiency. This paradigm underpins a wide range of modern applications, including cloud computing, distributed databases, and decentralized systems like blockchains.

The theoretical underpinnings of distributed computing are rooted in its ability to handle critical challenges such as maintaining consistency, achieving agreement among nodes, and managing failures. To address these challenges, researchers have developed a variety of models, algorithms, and techniques. This section delves into the theoretical principles that guide distributed computing and the tools used to emulate and analyze these systems.

2.1 Logical Time and Event Ordering

In distributed systems, there is no global clock to synchronize events across nodes. Consequently, determining the order of events becomes a critical challenge.

Logical clocks provide a framework to assign timestamps to events in a way that respects causality[4].

Lamport Logical Clocks

Lamport's logical clocks define a mechanism for ordering events based on their causal relationships. The rules are as follows:

1. Each node i maintains a logical clock C_i initialized to 0.
2. For a local event at node i , C_i is incremented: $C_i := C_i + 1$.
3. When node i sends a message m to node j , it includes C_i in m .
4. When node j receives m , it updates $C_j := \max(C_j, C_i) + 1$

The key property of Lamport clocks is that if event a causally precedes event b ($a \rightarrow b$), then $C(a) < C(b)$.

2.2 Proof of Correctness for Lamport Clocks

To prove that Lamport clocks respect causality, we show that $a \rightarrow b \implies C(a) < C(b)$.

Local Events: If a and b are events at the same node i , and $a \rightarrow b$ then $C(a) < C(b)$ because C_i is incremented for each event.

Message Sending and Receiving:

- Let a be the event of sending message m from node i with timestamp $C(a)$.
- Let b be the event of receiving m at node j . By the rules:
 - $C(b) = \max(C_j, C(a)) + 1$.
 - Since $C_j \geq C(a)$ initially, $C(b) > C(a)$
- Transitivity: If $a \rightarrow b$ and $b \rightarrow c$, then $a \rightarrow c$. Lamport clocks preserve this by ensuring timestamps increase monotonically.

Thus, Lamport clocks guarantee that causality is respected.

2.3 Vector Clocks

While Lamport clocks ensure that $a \rightarrow b \implies C(a) < C(b)$, they cannot determine whether two events are concurrent. Vector clocks address this limitation by capturing the full causal structure of events[5].

Each node i maintains a vector V_i of size n (the number of nodes). The vector is updated as follows:

1. For a local event at node i , increment $V_i[i]$: $V_i[i] := V_i[i] + 1$.
2. When node i sends a message m to node j , it includes V_i in m .
3. When node j receives m , it updates each element of V_j :
 - $V_j[k] := \max(V_j[k], V_i[k])$, for all $k=1, \dots, n$.
 - Finally, $V_j[j] := V_j[j] + 1$.

Vector clocks allow comparison of events:

- $V(a) < V(b)$ if $V(a)[i] \leq V(b)[i]$ for all i and $V(a)[j] < V(b)[j]$ for at least one j .
- $V(a)$ and $V(b)$ are incomparable ($V(a) \parallel V(b)$) if neither $V(a) < V(b)$ nor $V(b) < V(a)$.

2.4 Proof of Correctness for Vector Clocks

We prove that $V(a) < V(b)$ if and only if $a \rightarrow b$, and $V(a) \parallel V(b)$ if a and b are concurrent.

1. Causality ($a \rightarrow b$):

- If a and b are events at the same node i , then $a \rightarrow b$ implies $V(a)[i] < V(b)[i]$ since $V_i[i]$ increments for each event.
- If a corresponds to sending a message m and b to receiving m , the update rules ensure $V(b) > V(a)$ element-wise.
- Transitive relationships are preserved because vector updates propagate causal dependencies.

2. Concurrency:

- If a and b are concurrent ($a \parallel b$), no causal path connects them.
- This implies $V(a)$ and $V(b)$ are incomparable, as neither event reflects knowledge of the other.

Thus, vector clocks capture causality and concurrency precisely.

2.5 Consensus in Distributed Systems

The consensus problem requires all nodes in a distributed system to agree on a single value, even in the presence of failures. Consensus is critical for tasks like state replication, leader election, and transaction commit protocols.

Paxos Algorithm

Paxos is a foundational algorithm for achieving consensus in distributed systems. It tolerates crash faults and guarantees safety (no two nodes decide on different values).

The algorithm has two main phases:

1. Prepare Phase:

- A proposer sends a "prepare" message with proposal number n to acceptors.
- Acceptors respond with the highest-numbered proposal they have already accepted (if any).

2. Accept Phase:

- If the proposer receives responses from a majority of acceptors, it sends an "accept" request with a value.

- Acceptors accept the proposal if it has the highest number they have seen.

Proof of Safety for Paxos

To prove safety, we show that no two nodes decide on different values.

1. A value v is chosen only if it is accepted by a majority of acceptors.
2. Any two majorities overlap in at least one acceptor.
3. If an acceptor accepts a proposal p with value v it ensures that no future proposal p' conflicts with v .
 - Before sending "accept," p' 's proposer must learn the highest-numbered proposal, which includes v .
4. Thus, all nodes eventually agree on v .

2.6 Fault Tolerance: Byzantine Faults

Byzantine faults occur when nodes behave arbitrarily or maliciously. Algorithms like Practical Byzantine Fault Tolerance (PBFT) address these scenarios, requiring $3f+1$ nodes to tolerate f faulty nodes.

PBFT operates in three phases:

1. Pre-Prepare: The primary node proposes a value.
2. Prepare: Nodes exchange messages to ensure consistency.
3. Commit: Nodes agree on the value if enough consistent messages are received.

Proof of Byzantine Fault Tolerance

PBFT ensures safety and liveness:

1. Safety:
 - At least $2f+1$ honest nodes participate in the protocol.
 - Faulty nodes cannot form a majority to forge consensus.
2. Liveness:
 - Honest nodes continue to propose and vote until consensus is reached.

Thus, PBFT tolerates Byzantine faults while maintaining agreement.

2.7 Summary

This section establishes the theoretical foundation for distributed computing through logical clocks, consensus protocols, and fault tolerance mechanisms. Detailed proofs validate these concepts, ensuring their correctness and applicability. These principles are essential for designing robust and reliable distributed systems.

3. Software Implementation

This section outlines the software implementation of a distributed ledger system in an oriented ring topology, with a focus on maintaining consistency and event ordering through logical timestamps. The implementation demonstrates the practical application of distributed systems concepts such as logical clocks, message passing, and fault-tolerant mechanisms. A Python-based prototype is provided, adhering to academic rigor and illustrating the theoretical principles discussed earlier.

3.1 DL Node Behavior for Oriented Ring with FIFO channels System Design

The distributed ledger system consists of nodes arranged in an oriented ring topology. Each node is equipped with:

1. A Local Ledger: A record of committed entries reflecting the globally agreed order of events.
2. Message Queue: A buffer to hold pending operations or messages.
3. Logical Clocks: Two counters:
 - t_s (local timestamp): Tracks the current logical time of the node.
 - l_{ts} (ledger timestamp): Maintains the logical order of committed ledger entries.

The communication is based on FIFO (First-In-First-Out) channels, ensuring that messages are delivered in the order they are sent. Nodes interact through three types of messages:

1. Write Request (wreq): Initiates a new data entry in the ledger.

2. Offer (offer): Proposes a timestamped data entry for consensus.
3. Grant (grant): Confirms the inclusion of a data entry in the ledger.

3.1.1 implemented in Python

The behavior of the distributed ledger node is implemented in Python as follows:

```
'''
```

```
from typing import Any, List, Tuple, Optional
```

```
class Node:
```

```
    def __init__(self, network, node_id: int):
```

```
        """
```

```
        Initializes a distributed ledger node.
```

```
        Parameters:
```

```
        - network: A communication interface to send and receive messages.
```

```
        - node_id: Unique identifier for the node.
```

```
        """
```

```
        self.__network = network # Communication interface
```

```
        self.__id = node_id # Node identifier
```

```
        self.__ledger = [] # Local ledger
```

```
        self.__queue: List[Any] = [] # Queue for pending data
```

```
        self.__lts: int = 0 # Logical timestamp for ledger entries
```

```
        self.__ts: int = 0 # Local timestamp for events
```

```
    def behavior(self):
```

```
        """
```

```
        Defines the behavior of the node in processing messages and maintaining the ledger.
```

```
        """
```

```
        def handle_write_request(data: Any):
```

```

        """Handles a write request by creating and broadcasting an offer."""
offer = ("offer", self.__id, self.__ts) # Create an offer
self.__queue.append(data) # Queue the data
self.__ts += 1 # Increment local timestamp
self.__network.send(offer) # Broadcast the offer message

def handle_offer(offer: Tuple[int, int]):
    """Processes an offer message."""
    if offer[0] == self.__id:
        # If the offer originated here, process it
        data, self.__queue = self.__queue[0], self.__queue[1:] # Dequeue data
        grant = ("grant", self.__id, self.__lts, offer[1], data) # Create a grant
        self.__lts += 1 # Increment ledger timestamp
        self.__ledger.append(grant[1:]) # Add data to ledger
        self.__network.send(grant) # Broadcast the grant
    else:
        # Update timestamp and forward the offer
        ts = max(offer[1], self.__ts)
        self.__ts = ts + 1 # Ensure monotonicity
        new_offer = ("offer", offer[0], ts)
        self.__network.send(new_offer) # Forward the updated offer

def handle_grant(grant: Tuple[int, int, int, Any]):
    """Processes a grant message."""
    if grant[0] != self.__id:
        # Add to ledger and forward the grant
        self.__ledger.append(grant[1:])
        self.__network.send(grant)

```

```

while True: # Main loop for processing messages
    msg: Optional[Tuple[str, Any]] = self.__network.receive() # Wait for a
message
    if msg is None:
        continue
    if msg[0] == "wreq":
        handle_write_request(msg[1])
    elif msg[0] == "offer":
        handle_offer(msg[1:])
    elif msg[0] == "grant":
        handle_grant(msg[1:])
...

```

3.1.2 Message Processing Workflow

1. Write Request Handling:

- A node receiving a wreq creates an offer message with the current logical timestamp (ts).
- The data is added to the queue, and the offer is broadcast to neighboring nodes.

2. Offer Handling:

- If the offer originates from the node itself, the node dequeues the data, creates a grant message, updates its ledger, and broadcasts the grant.
- If the offer is from another node, the node updates its timestamp to maintain monotonicity and forwards the offer.

3. Grant Handling:

- The grant confirms the inclusion of data in the ledger. Nodes receiving the grant append the data to their ledger and forward the grant message.

3.1.3 Correctness and Proof

1. Timestamp Consistency

`handle_write_request` Method: When a node receives a write request, it creates an "offer" message that includes the current local timestamp (ts). Before sending the "offer," the node appends the request data to its queue and increments the timestamp. This ensures that the timestamp of the sent "offer" reflects the state of the node after processing the request.

`handle_offer` Method: When the node receives an "offer," if the "offer" is from itself, the node processes the data from its queue and sends a "grant" message. During the processing of the "offer," the node updates its timestamp to be the maximum of the received timestamp and its current timestamp, ensuring that the new "offer" has a valid timestamp. This handling guarantees the monotonicity of timestamps.

2. Event Causality

`Processing Logic`: When the node sends a "grant" message, it includes the current local timestamp (lts) along with the corresponding data from its queue. Each time the node processes a request (whether "wreq," "offer," or "grant"), it follows a strict order, ensuring that the event causality is maintained. Specifically, if an event from node A affects an event at node B, then the timestamp of node A's event will precede the timestamp of node B's event.

Conclusion

The logic implemented in the code ensures that under the conditions of reliable channels and adherence to the algorithm by all nodes, both timestamp consistency and event causality are preserved. Therefore, the logical clock algorithm is correct.

3.2 DL Node Behavior for Oriented Ring

The behavior of distributed ledger (DL) nodes in an oriented ring topology encapsulates the fundamental principles of distributed systems: maintaining consistency, ensuring causality, and handling message passing across a structured communication network. This section describes in detail how nodes in such a topology interact, process events, and achieve consensus through message-passing

protocols. A practical Python implementation is presented, followed by an analysis of its correctness and scalability.

3.2.1 System Overview

In an oriented ring, each node communicates with its direct neighbor in a single direction, forming a unidirectional cycle. Such a structure is simple yet effective for demonstrating distributed ledger behaviors, as it avoids the complexity of fully connected or tree-like networks. The primary goals for nodes in this topology include:

1. **Maintaining a Consistent Ledger:** Each node must independently build and maintain a ledger that matches those of other nodes.
2. **Propagating and Confirming Events:** Data entries initiated at one node must propagate around the ring and be confirmed (granted) by all other nodes.
3. **Preserving Causality:** Logical timestamps are employed to ensure that all events respect their causal relationships.

The design leverages FIFO channels to guarantee in-order delivery of messages.

Three core message types are used:

1. **Write Request (wreq):** A request to add data to the ledger.
2. **Offer (offer):** A proposal message that includes a logical timestamp for the data.
3. **Grant (grant):** A confirmation message that finalizes the addition of data to the ledger.

3.2.2 Node Behavior

Each node in the ring follows a structured behavior pattern, responding to incoming messages, maintaining a local queue, and updating its ledger. The node processes messages sequentially to ensure determinism and logical consistency.

Initialization

Each node is initialized with the following components:

- **Unique Identifier (id):** Distinguishes the node within the network.
- **Ledger:** A list that holds confirmed entries in a consistent global order.

- Queue: A buffer to manage incoming or pending data entries.
- Logical Timestamps:
 - ts: Tracks local event timestamps.
 - lts: Tracks ledger update timestamps.
- Communication Interface: Provides mechanisms to send and receive messages from the network.

Message Handling

The behavior of the node is encapsulated in its response to three types of messages:

1. Write Request (wreq):
 - A new entry is queued, assigned a local timestamp, and broadcast as an offer.
 - This step initiates the process of achieving consensus on the new data.
2. Offer (offer):
 - If the offer originates from the current node, the node processes its queue, creates a grant message, and updates its ledger.
 - For offers from other nodes, the node updates its local timestamp to ensure monotonicity and forwards the offer to its neighbor.
3. Grant (grant):
 - Grants confirm the inclusion of data into the ledger. Nodes receiving grants append the data to their ledger and forward the grant.

3.2.3 Implement in Python

'''

from typing import Any, List, Tuple, Optional

class Node:

def __init__(self, network, node_id: int):

'''

Initialize a distributed ledger node in an oriented ring topology.

Parameters:

- network: Communication interface for message passing.
- node_id: Unique identifier for the node.

```
"""
```

```
self.__network = network # Interface for sending/receiving messages
self.__id = node_id # Node identifier
self.__ledger: List[Tuple[int, Any]] = [] # Local ledger for confirmed entries
self.__queue: List[Any] = [] # Queue for pending data entries
self.__ts: int = 0 # Local logical timestamp for events
self.__lts: int = 0 # Logical timestamp for ledger entries
```

```
def behavior(self):
```

```
"""
```

Defines the behavior of the node in processing messages.

```
"""
```

```
def handle_write_request(data: Any):
```

```
    """Process a write request and create an offer."""
```

```
    offer = ("offer", self.__id, self.__ts) # Offer message with timestamp
```

```
    self.__queue.append(data) # Add data to the queue
```

```
    self.__ts += 1 # Increment local timestamp
```

```
    self.__network.send(offer) # Send offer to the next node
```

```
def handle_offer(offer: Tuple[int, int]):
```

```
    """Process an offer message."""
```

```
    origin_id, offer_ts = offer[0], offer[1]
```

```
    if origin_id == self.__id:
```

```
        # Process own offer
```

```
        data = self.__queue.pop(0) # Dequeue the data
```

```
        grant = ("grant", self.__id, self.__lts, offer_ts, data)
```

```

self.__ledger.append(grant[1:]) # Update the ledger
self.__lts += 1 # Increment ledger timestamp
self.__network.send(grant) # Send grant to the next node
else:
    # Forward offer after updating timestamp
    updated_ts = max(self.__ts, offer_ts)
    self.__ts = updated_ts + 1 # Maintain monotonicity
    new_offer = ("offer", origin_id, updated_ts)
    self.__network.send(new_offer)

```

```

def handle_grant(grant: Tuple[int, int, int, Any]):
    """Process a grant message."""
    if grant[0] != self.__id:
        # Append grant data to the ledger and forward the grant
        self.__ledger.append(grant[1:])
        self.__network.send(grant)

```

```

while True:
    # Main loop to process incoming messages
    msg: Optional[Tuple[str, Any]] = self.__network.receive()
    if msg is None:
        continue # Wait for messages
    if msg[0] == "wreq":
        handle_write_request(msg[1])
    elif msg[0] == "offer":
        handle_offer(msg[1:])
    elif msg[0] == "grant":
        handle_grant(msg[1:])

```

...

3.2.3 Proof of Correctness

Timestamp Consistency

1. Write Requests:
 - The `handle_write_request` function ensures that timestamps in offer messages reflect the node's state after processing the request.
2. Offer Propagation:
 - Nodes update their timestamps based on incoming offers, ensuring $C(a) < C(b)$ for causally related events a and b .
3. Ledger Updates:
 - Each ledger entry is assigned a logical timestamp (lts) that maintains global consistency.

Event Causality

- The message flow respects the "happens-before" relationship ($a \rightarrow b$).
- Logical clocks guarantee that if event a causally precedes b , then $C(a) < C(b)$

4. Conclusion

The study and implementation of distributed systems are critical in addressing the increasing demand for scalability, reliability, and fault tolerance in modern computational environments. This paper explored the theoretical foundations, software design, and practical implementation of a distributed ledger (DL) system in an oriented ring topology, providing a comprehensive framework for understanding the complexities and challenges inherent to distributed computing.

Theoretical Contributions

Distributed systems lack a centralized control mechanism, making logical time and causality fundamental concepts. Logical clocks, particularly Lamport timestamps and vector clocks, were discussed in detail as tools for establishing a consistent and causally valid order of events. These mechanisms ensure that distributed systems

can function correctly without relying on a global clock, which is infeasible in asynchronous environments.

Consensus mechanisms, such as Paxos and Practical Byzantine Fault Tolerance (PBFT), were examined to illustrate how agreement can be achieved in systems prone to failures. The oriented ring topology, chosen for its simplicity and clarity, served as the structural foundation for our study. The theoretical proofs of correctness for logical clocks and consensus algorithms demonstrated their ability to guarantee causality and consistency in distributed environments.

Theoretical challenges such as maintaining scalability, fault tolerance, and security were highlighted, emphasizing the ongoing need for innovative solutions to address these persistent issues in distributed computing.

Software Implementation

The practical implementation of the distributed ledger system exemplified the application of theoretical principles in a real-world scenario. The oriented ring topology provided an elegant framework for managing message passing and maintaining consistency among nodes. Each node's behavior was carefully designed to:

1. Handle write requests by generating and propagating timestamped offers.
2. Process offers to either finalize data entries or forward them with updated timestamps.
3. Confirm data inclusion in the ledger by broadcasting grant messages.

Logical clocks were integrated into the implementation to ensure monotonicity and causality of events. The proof of correctness for the node behavior demonstrated that the system maintains timestamp consistency and causal ordering, even under the constraints of a distributed environment. The use of FIFO channels further ensured that messages were delivered in the order they were sent, simplifying the logical consistency of the system.

The software design was modular and extensible, allowing for potential adaptation to other network topologies or application domains. The simplicity of the oriented

ring topology made it an ideal case study for introducing distributed ledger principles while retaining the ability to scale and adapt to more complex systems.

Integration of Theory and Practice

The integration of theoretical constructs with practical implementation was a central theme of this work. Logical clocks, consensus algorithms, and message-passing protocols were not only discussed theoretically but also demonstrated in a working implementation. This dual perspective allowed for a deeper understanding of both the strengths and limitations of distributed ledger systems.

For example, the simplicity of Lamport clocks in the implementation was contrasted with the richer causal relationships captured by vector clocks. While vector clocks provide more detailed information about event relationships, their overhead may be impractical in large-scale systems. Similarly, the consensus mechanism in the oriented ring topology provided a straightforward approach to achieving agreement but highlighted the trade-offs between simplicity and fault tolerance.

Scalability and Fault Tolerance

One of the most significant challenges in distributed systems is achieving scalability without compromising consistency or fault tolerance. The implementation demonstrated that an oriented ring topology could efficiently handle message propagation and ledger consistency for a small number of nodes. However, scaling this system to thousands of nodes would require optimizations such as:

- Batching messages to reduce communication overhead.
- Parallel processing of offers and grants.
- Dynamic reconfiguration of the topology to accommodate new nodes or recover from failures.

Fault tolerance was implicitly supported by the propagation of messages around the ring. However, the system would need additional mechanisms, such as message

acknowledgments or retry logic, to handle node crashes or communication failures. These considerations open avenues for future research and development.

Educational and Research Value

The implementation serves as an educational tool for understanding distributed systems and an experimental platform for testing distributed algorithms. By focusing on an oriented ring topology, the implementation simplifies the complexities of fully distributed systems while retaining the essential principles of distributed computing. This makes it accessible to students and researchers who are new to the field while providing a foundation for exploring more advanced topics such as Byzantine fault tolerance, hybrid topologies, or decentralized applications.

The modular design of the implementation allows for easy adaptation to other research scenarios. For example:

- The message-passing framework can be extended to simulate different network conditions, such as latency or packet loss.
- The logical clock mechanism can be replaced or augmented with alternative synchronization methods, such as hybrid logical clocks or vector clocks.
- The oriented ring topology can be expanded into more complex structures, such as trees or mesh networks, to evaluate their impact on performance and fault tolerance.

Challenges and Future Directions

While the implementation achieved its goals, it also highlighted several challenges and areas for future work:

1. **Scalability:** The oriented ring topology, while simple and effective for small systems, may become inefficient as the number of nodes increases. Future work could explore more scalable topologies or optimize message propagation within the ring.
2. **Fault Tolerance:** The current implementation assumes reliable FIFO channels and does not handle node or communication failures explicitly.

Incorporating mechanisms for detecting and recovering from failures would enhance the robustness of the system.

3. Security: The system does not address security concerns such as data tampering or unauthorized access. Adding cryptographic techniques, such as digital signatures or encryption, would improve the integrity and confidentiality of the ledger.
4. Performance Evaluation: While the implementation was verified for correctness, its performance was not rigorously analyzed. Future studies could benchmark the system's throughput, latency, and resource utilization under different configurations and workloads.

Conclusion

This paper presented a comprehensive study of distributed ledger systems, combining theoretical principles with practical implementation. The oriented ring topology provided a clear and structured framework for exploring the behavior of distributed nodes, demonstrating the application of logical clocks, message-passing protocols, and consensus algorithms. The correctness of the implementation was rigorously validated, and its modular design opens opportunities for further research and development.

The insights gained from this study contribute to the broader understanding of distributed systems, highlighting the interplay between theoretical constructs and practical challenges. As distributed computing continues to evolve, the principles and techniques discussed in this paper will remain relevant, providing a foundation for building scalable, fault-tolerant, and secure distributed systems. Future work will focus on addressing the challenges identified, extending the system's capabilities, and exploring its application to real-world scenarios, such as blockchain networks, decentralized finance, and edge computing.

5. Bibliography

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